

Q# 12, 22 + P# 13, 14, 16, 19

Q# 12

impulse momentum

$$J = \Delta P$$

★ Newton's 3rd law
action/reaction pairs

$$J_{x_1} = J_{x_2}$$

$$\Delta P_1 = (P_f)_1 - (P_i)_1$$

$$\Delta P_2 = (P_f)_2 - (P_i)_2$$

Q #22

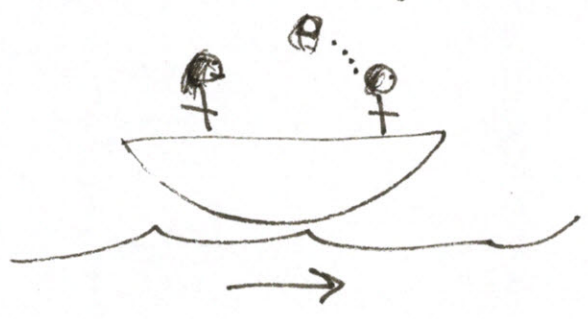
(A)

$t_i = 3.0s$

$t_f = 3.2s$

$v_i = 0 \text{ m/s}$

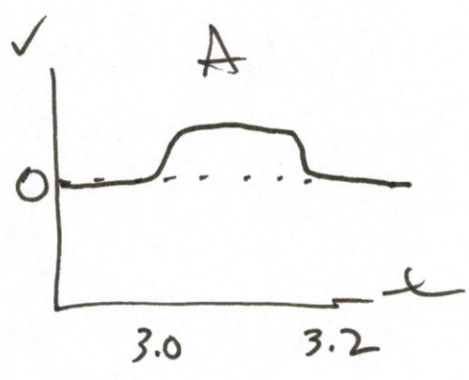
sack travels in the opposite direction ($= -P$)



isolated system

$P_{x_i} = \phi$

$-P = P$
sack in air canoe



NAME

Period

P #13

before 0.100kg

$m_1 = 100g$ small

$v_1 = 1.20 m/s$

$m_2 = 1.0 kg$ large

$v_2 = 0 m/s$

after

$m_1 = 0.100kg$

$v_1 = -0.850 m/s$

$m_2 = 1.0 kg$

$v_2 = ?$

$$(P_x)_i = (P_x)_f$$

$$(P_{1x})_i + (P_{2x})_i = (P_{1x})_f + (P_{2x})_f$$

$$(m_1 v_{1x})_i + (m_2 v_{2x})_i = (m_1 v_{1x})_f + (m_2 v_{2x})_f$$

$$v_{2x} = \frac{(m_1 v_{1x})_i + (m_2 v_{2x})_i - (m_1 v_{1x})_f}{m_2}$$

$$\frac{(0.100kg)(1.20 m/s) - (0.100kg)(-0.850 m/s)}{1.0 kg}$$

$$\frac{0.205}{1.0}$$

$v_2 = 0.205 m/s$

P
 #14
 $m_1 = 70 \text{ kg}$
 man + rifle
 $m_2 = 0.01 \text{ kg}$
 bullet
 $v_2 = 500 \text{ m/s}$
 $v_1 = ?$
 man

isolated system
 (no external
 force)

$$\begin{aligned}
 (P_x)_i &= (P_x)_f \\
 (P_{1x})_f + (P_{2x})_f &= (P_{1x})_i + (P_{2x})_i \\
 (m_1 v_1)_f + (m_2 v_2)_f &= (m_1 v_1)_i + (m_2 v_2)_i = 0
 \end{aligned}$$

$$\begin{aligned}
 (v_1)_f &= - \left(\frac{m_2}{m_1} \right) (v_2)_f = \\
 &= - \left(\frac{0.01 \text{ kg}}{70 \text{ kg}} \right) (500 \text{ m/s}) \\
 &= -0.0001429 \\
 &= \text{---} (500)
 \end{aligned}$$

$$(v_1)_f = -0.071 \text{ m/s}$$

P
16

before
$m_1 - 5.3 \text{ kg}$
$m_2 - 2.3 \text{ kg}$
$v_{1+2} - 0 \text{ m/s}$

after
$m_1 - 5.3 \text{ kg}$
$m_2 - 2.3 \text{ kg}$
$v_1 - ?$
$v_2 - 6.0 \text{ m/s}$

$$(v_{1x})_f = - \left(\frac{m_2}{m_1} \right) (v_{2x})_f$$
$$= \left(\frac{2.3 \text{ kg}}{5.3 \text{ kg}} \right) (6.0 \text{ m/s})$$
$$= 0.4339 (6.0)$$

$$(v_{1x})_f = \boxed{-2.6 \text{ m/s}}$$

P
#19

$$m_1 = 55 \text{ kg}$$

$$m_2 = \cancel{42 \text{ g}} \quad 0.042 \text{ kg}$$

$$(v_2)_f = 620 \text{ m/s}$$

$$(v_1)_i = 0 \text{ m/s}$$

$$(m_1 v_1)_f + (m_2 v_2)_f = (m_1 v_1)_i + (m_2 v_2)_i = 0$$

$$(v_1)_f = -\left(\frac{m_2}{m_1}\right)(v_2)_f$$

$$= -\left(\frac{0.042 \text{ kg}}{55 \text{ kg}}\right)(620 \text{ m/s})$$

$$= -0.0007636 (620)$$

$$(v_1)_f = -0.47 \text{ m/s}$$